

# An Introduction to Event History Analysis

Oxford Spring School

June 18-20, 2007

Day Two: Regression Models for Survival Data

Figure 1: Various Functions of an Exponential Model with  $\lambda = 0.02$

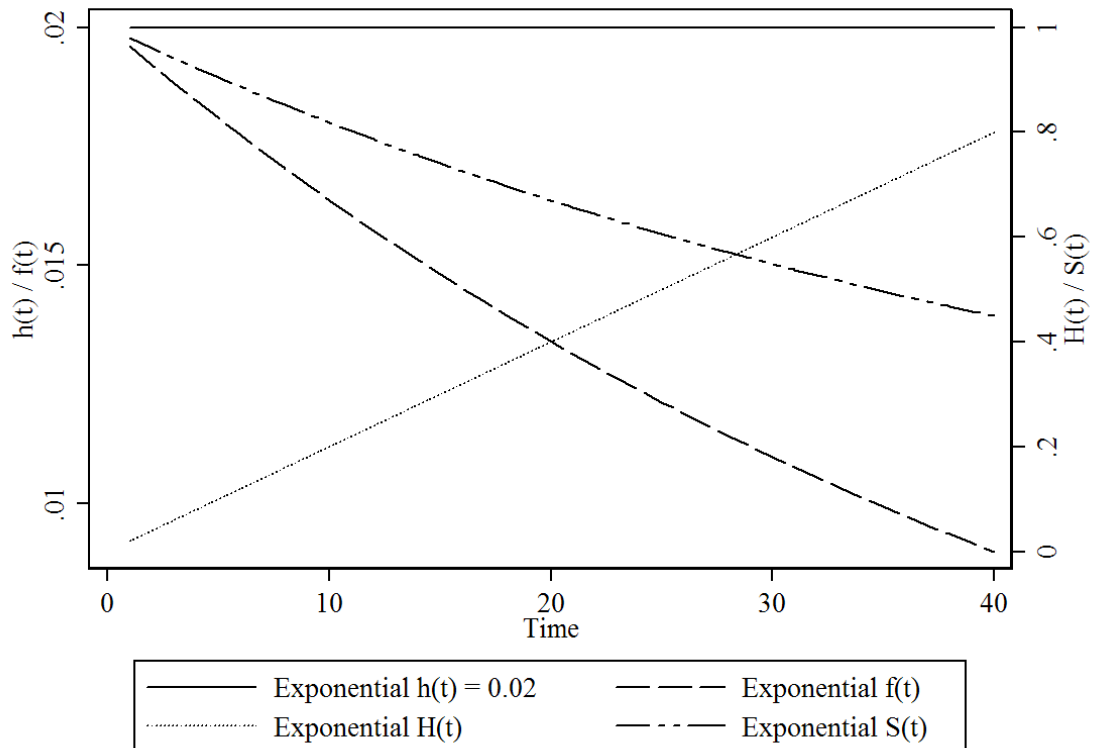


Figure 2: Various Weibull Hazards with  $\lambda = 0.02$

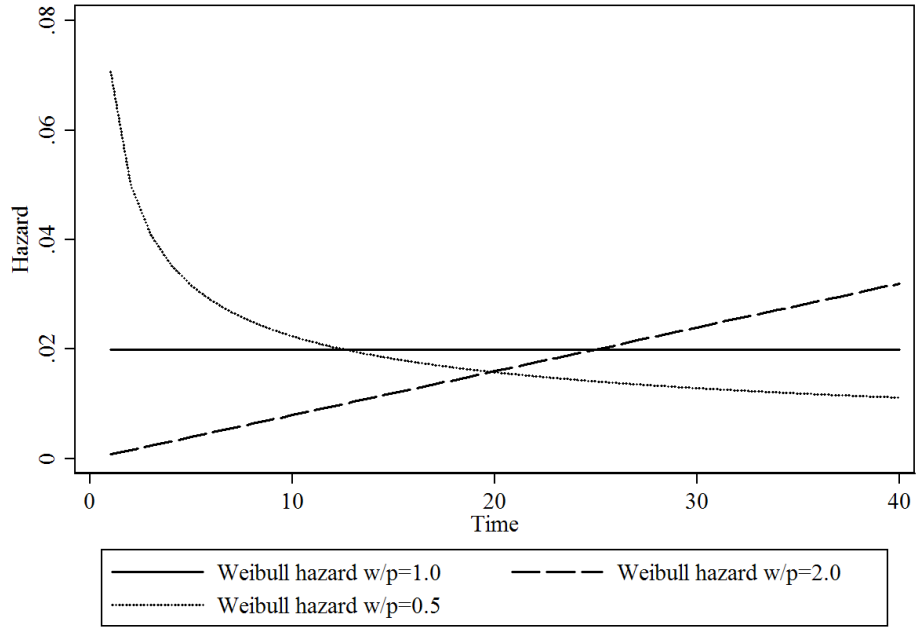


Figure 3: Various Weibull Survival Functions with  $\lambda = 0.02$

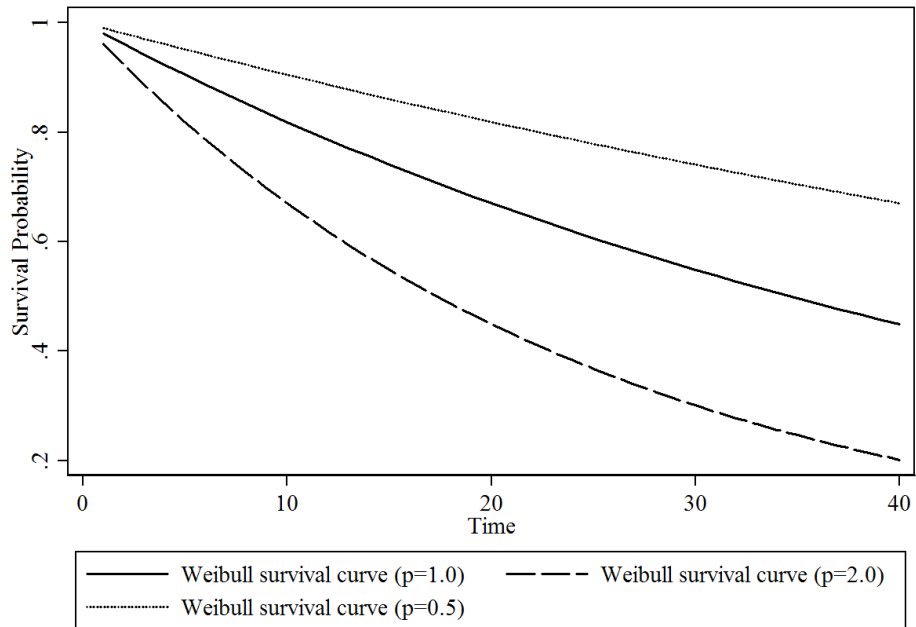


Figure 4: Various Gompertz Hazards with  $\lambda = 0.001$

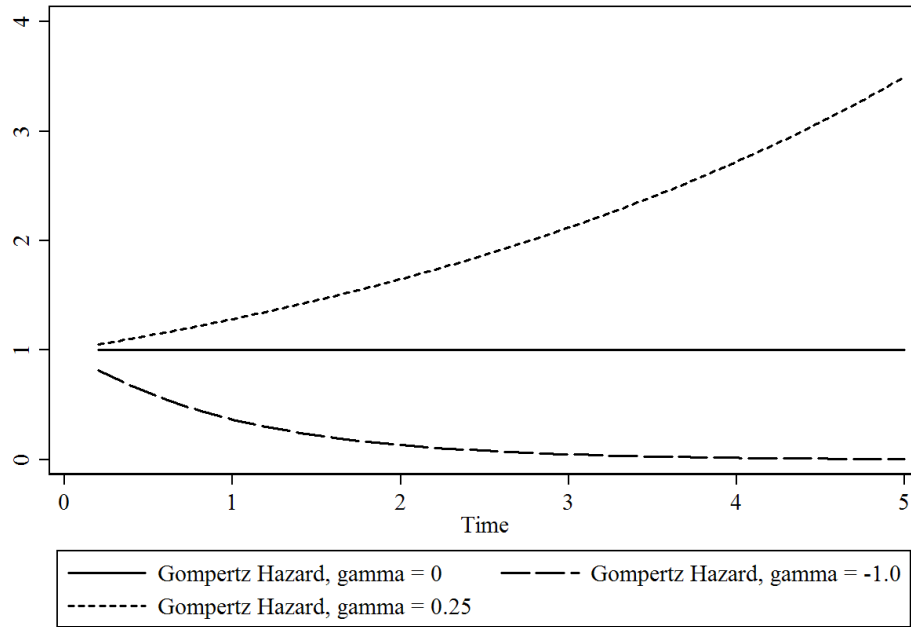
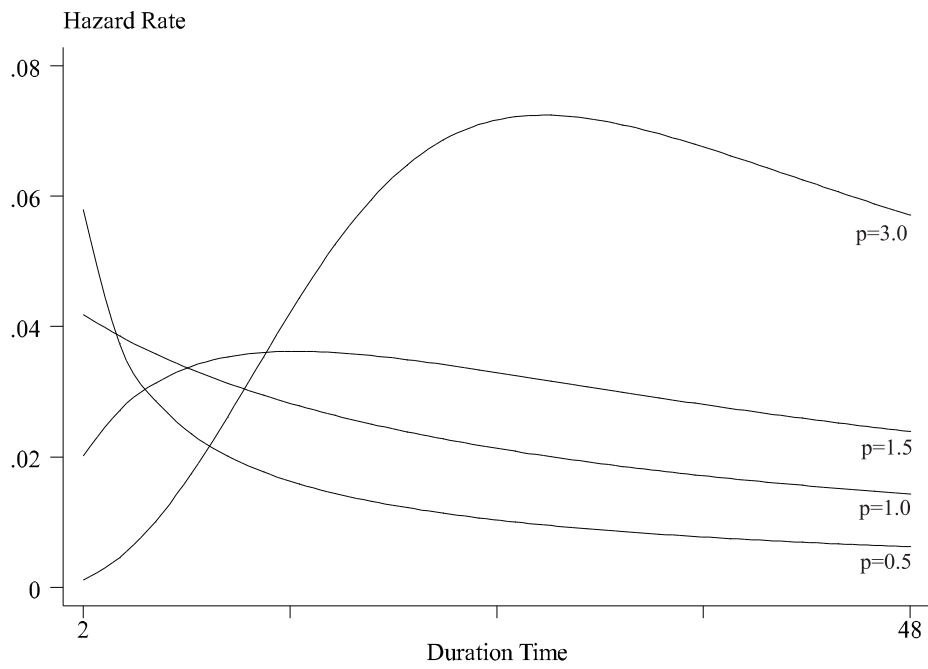


Figure 5: Various Log-Logistic Hazards



**Example: Supreme Court Retirements, 1789-1992**

. summarize justice service retire age pension pagree

Variable	Obs	Mean	Std. Dev.	Min	Max
justice	1765	52.13144	29.53513	1	107
service	1765	11.74391	8.338646	1	37
retire	1765	.0288952	.1675594	0	1
age	1765	62.09518	9.647412	32	91
pension	1765	.1988669	.3992607	0	1
pagree	1765	.6164306	.4863928	0	1

. stdes

failure \_d: retire  
analysis time \_t: service  
id: justice

Category	total	per subject			
		mean	min	median	max
no. of subjects	107				
no. of records	1765	16.49533	2	16	37
(first) entry time		0	0	0	0
(final) exit time		16.61682	2	16	37
subjects with gap	0				
time on gap if gap	0	.	.	.	.
time at risk	1778	16.61682	2	16	37
failures	51	.4766355	0	0	1

. stvary

failure \_d: retire  
analysis time \_t: service  
id: justice

subjects for whom the variable is

variable	constant	varying	never	always	sometimes
			missing	missing	missing
age	0	107	107	0	0
pension	60	47	107	0	0
pagree	28	79	107	0	0

*Exponential Models, Constant-Only:*

Hazard rate form:

```
. streg , nohr dist(exp)
```

Exponential regression -- log relative-hazard form

```
No. of subjects =          107          Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood  = -100.83092          LR chi2(0)        =          -0.00
                                          Prob > chi2       =           .
```

---

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
-----+-----						
_cons	-3.551419	.140028	-25.36	0.000	-3.825869	-3.276969

---

AFT form:

```
. streg , time dist(exp)
```

Exponential regression -- accelerated failure-time form

```
No. of subjects =          107          Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood  = -100.83092          LR chi2(0)        =          -0.00
                                          Prob > chi2       =           .
```

---

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
-----+-----						
_cons	3.551419	.140028	25.36	0.000	3.276969	3.825869

---

*Exponential Models, With Covariates:*

```
. streg age pension pagree, nohr dist(exp)
```

Exponential regression -- log relative-hazard form

```
No. of subjects =          107                Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood   =  -78.351408                LR chi2(3)        =          44.96
                                                Prob > chi2       =          0.0000
```

---

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.041146	.0210568	1.95	0.051	-.0001246	.0824165
pension	1.321105	.3870769	3.41	0.001	.5624487	2.079762
pagree	.1069193	.2854665	0.37	0.708	-.4525849	.6664234
_cons	-6.837742	1.341503	-5.10	0.000	-9.467039	-4.208445

---

```
. streg age pension pagree, time dist(exp)
```

Exponential regression -- accelerated failure-time form

```
No. of subjects =          107                Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood   =  -78.351408                LR chi2(3)        =          44.96
                                                Prob > chi2       =          0.0000
```

---

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	-.041146	.0210568	-1.95	0.051	-.0824165	.0001246
pension	-1.321105	.3870769	-3.41	0.001	-2.079762	-.5624487
pagree	-.1069193	.2854665	-0.37	0.708	-.6664234	.4525849
_cons	6.837742	1.341503	5.10	0.000	4.208445	9.467039

---

*Weibull Models, With Covariates:*

```
. streg age pension pagree, nohr dist(weib)
```

Weibull regression -- log relative-hazard form

```
No. of subjects =          107                Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood  =  -78.350319                LR chi2(3)         =          26.79
                                                Prob > chi2        =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.0405689	.0244068	1.66	0.096	-.0072675	.0884052
pension	1.317683	.3935936	3.35	0.001	.5462542	2.089113
pagree	.1084476	.2872933	0.38	0.706	-.4546368	.6715321
_cons	-6.83356	1.344091	-5.08	0.000	-9.46793	-4.19919
/ln_p	.0103713	.2216177	0.05	0.963	-.4239915	.444734
p	1.010425	.2239281			.6544294	1.560075
1/p	.9896823	.2193312			.6409947	1.528049

```
. streg age pension pagree, time dist(weib)
```

Weibull regression -- accelerated failure-time form

```
No. of subjects =          107                Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood  =  -78.350319                LR chi2(3)         =          26.79
                                                Prob > chi2        =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	-.0401503	.0296687	-1.35	0.176	-.0982999	.0179993
pension	-1.304088	.5264274	-2.48	0.013	-2.335867	-.2723093
pagree	-.1073287	.2826184	-0.38	0.704	-.6612506	.4465932
_cons	6.763054	2.0678	3.27	0.001	2.710241	10.81587
/ln_p	.0103713	.2216177	0.05	0.963	-.4239915	.444734
p	1.010425	.2239281			.6544294	1.560075
1/p	.9896823	.2193312			.6409947	1.528049

*Gompertz Model:*

```
. streg age pension pagree, nohr dist(gompertz)
```

Gompertz regression -- log relative-hazard form

```
No. of subjects =          107          Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood   =  -78.342685          LR chi2(3)       =          26.31
                                          Prob > chi2     =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.0430369	.0255498	1.68	0.092	-.0070398	.0931136
pension	1.329599	.3932018	3.38	0.001	.5589376	2.10026
pagree	.1049069	.2859234	0.37	0.714	-.4554928	.6653065
_cons	-6.920901	1.487491	-4.65	0.000	-9.83633	-4.005471
gamma	-.0031625	.0239883	-0.13	0.895	-.0501787	.0438538



*Log-Logistic and Log-Normal Models:*

```
. streg age pension pagree, dist(loglog)
```

Log-logistic regression -- accelerated failure-time form

```
No. of subjects =          107                Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood  = -84.359393                LR chi2(3)         =          19.36
                                                Prob > chi2        =          0.0002
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	.0142307	.0220574	0.65	0.519	-.029001	.0574624
pension	-2.846252	3.764288	-0.76	0.450	-10.22412	4.531617
pagree	.0806037	.4969815	0.16	0.871	-.8934623	1.05467
_cons	2.770183	1.381703	2.00	0.045	.0620944	5.478271
/ln_gam	-.38227	.2162617	-1.77	0.077	-.8061351	.041595
gamma	.6823108	.1475577			.4465807	1.042472

```
. streg age pension pagree, dist(lognorm)
```

Log-normal regression -- accelerated failure-time form

```
No. of subjects =          107                Number of obs   =          1765
No. of failures =           51
Time at risk    =          1778
Log likelihood  = -81.42114                LR chi2(3)         =          26.77
                                                Prob > chi2        =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
age	-.0124893	.029725	-0.42	0.674	-.0707492	.0457705
pension	-3.598691	1.642479	-2.19	0.028	-6.817891	-.379491
pagree	.0354144	.4266008	0.08	0.934	-.8007078	.8715367
_cons	4.632599	1.873923	2.47	0.013	.9597768	8.305422
/ln_sig	.3819538	.2020201	1.89	0.059	-.0139983	.777906
sigma	1.465144	.2959887			.9860992	2.176909

## Brooks (2005): The Politics of Pension Privatisation

### Summary Statistics:

. stdes

```

failure _d: fail
analysis time _t: end
id: id

```

Category	total	per subject			
		mean	min	median	max
no. of subjects	59				
no. of records	896	15.18644	2	19	20
(first) entry time		3.254237	0	0	12
(final) exit time		18.44068	2	20	20
subjects with gap	0				
time on gap if gap	0	.	.	.	.
time at risk	896	15.18644	2	19	20
failures	18	.3050847	0	0	1

```

. su _d _t peerprivat LatinAm EEurCentAs LatAmxPeer EECaxPeer worldbank trade
infdi age65 parties fhouse partdem deficit mcap gdp cap lngdp

```

Variable	Obs	Mean	Std. Dev.	Min	Max
_d	896	.0200893	.1403841	0	1
_t	896	10.82478	5.757821	1	20
peerprivat	884	9.910966	10.44404	0	42.10526
LatinAm	896	.3772321	.4849645	0	1
EEurCentAs	896	.1383929	.3455047	0	1
LatAmxPeer	884	4.393904	9.233826	0	42.10526
EECaxPeer	884	.8908371	4.501443	0	31.25
worldbank	885	.0729091	.4845149	-7.25	3.75
trade	876	67.37009	38.91518	11.54567	238.7001
infdi	857	1.577509	2.092835	-1.223001	20.43747
age65	896	9.73256	4.683838	2.501285	17.86749
parties	878	3.4309	1.808586	0	16.25
fhouse	894	1.977629	1.374684	1	7
partdem	877	6.388198	5.722833	0	48.75
deficit	896	-3.571239	4.210995	-35.56053	8.988749
mcap	896	15.54599	34.78511	0	541.7224
gdp cap	863	10092.12	7369.03	1396.16	42769.14
lngdp	885	24.59823	1.974726	20.73322	29.84477

*Parametric Models*

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaXPeer worldbank trade
infdi age65 parties fhouse partdem deficit mcap gdpicap lngdp, nohr dist(exp)
```

Exponential regression -- log relative-hazard form

```
No. of subjects =          58                Number of obs   =          803
No. of failures =          18
Time at risk    =          803

Log likelihood =   -15.21816                LR chi2(16)      =          48.72
                                          Prob > chi2     =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
peerprivat	.0036511	.0714422	0.05	0.959	-.136373	.1436752
LatinAm	-.495087	1.789928	-0.28	0.782	-4.003282	3.013108
EEurCentAs	1.586211	1.418809	1.12	0.264	-1.194604	4.367026
LatAmxPeer	.1220979	.0844656	1.45	0.148	-.0434516	.2876474
EECaXPeer	.0608916	.081445	0.75	0.455	-.0987377	.2205209

(control variables omitted)

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaXPeer worldbank trade infdi
age65 parties fhouse partdem deficit mcap gdpicap lngdp, nohr dist(weibull)
```

Weibull regression -- log relative-hazard form

```
No. of subjects =          58                Number of obs   =          803
No. of failures =          18
Time at risk    =          803

Log likelihood =   -13.319909                LR chi2(16)      =          43.42
                                          Prob > chi2     =          0.0002
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
peerprivat	-.0510898	.0781423	-0.65	0.513	-.204246	.1020664
LatinAm	-.9050964	1.827672	-0.50	0.620	-4.487269	2.677076
EEurCentAs	.3484389	1.628047	0.21	0.831	-2.842475	3.539353
LatAmxPeer	.1565934	.0882266	1.77	0.076	-.0163276	.3295145
EECaXPeer	.1042015	.0865724	1.20	0.229	-.0654773	.2738802

(control variables omitted)

/ln_p	.6882986	.293876	2.34	0.019	.1123122	1.264285
p	1.990326	.5849091			1.118862	3.54056
1/p	.5024302	.1476522			.2824412	.8937652

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaXPeer worldbank trade infdi
age65 parties fhouse partdem deficit mcap gdpicap lngdp, dist(logn)
```

Log-normal regression -- accelerated failure-time form

```
No. of subjects =          58                Number of obs   =          803
No. of failures =          18
Time at risk    =          803

Log likelihood = -15.223621                LR chi2(16)      =          43.74
                                          Prob > chi2     =          0.0002
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
peerprivat	.0348855	.0260819	1.34	0.181	-.016234	.086005
LatinAm	.8293546	.7696259	1.08	0.281	-.6790845	2.337794
EEurCentAs	.6412098	.6137123	1.04	0.296	-.5616441	1.844064
LatAmxPeer	-.0679468	.0375044	-1.81	0.070	-.141454	.0055605
EECaXPeer	-.0733809	.0466923	-1.57	0.116	-.1648961	.0181343
(control variables omitted)						
/ln_sig	-.7035232	.3330094	-2.11	0.035	-1.35621	-.0508367
sigma	.4948388	.164786			.2576354	.9504338

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaXPeer worldbank trade infdi
age65 parties fhouse partdem deficit mcap gdpicap lngdp, dist(loglog)
```

Log-logistic regression -- accelerated failure-time form

```
No. of subjects =          58                Number of obs   =          803
No. of failures =          18
Time at risk    =          803

Log likelihood = -14.309971                LR chi2(16)      =          42.49
                                          Prob > chi2     =          0.0003
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
peerprivat	.0346197	.0263019	1.32	0.188	-.0169311	.0861706
LatinAm	.438246	.6020244	0.73	0.467	-.7417002	1.618192
EEurCentAs	.9684151	.6942763	1.39	0.163	-.3923416	2.329172
LatAmxPeer	-.0574358	.0311272	-1.85	0.065	-.1184441	.0035725
EECaXPeer	-.1731516	.0915367	-1.89	0.059	-.3525602	.0062571
(control variables omitted)						
/ln_gam	-1.385553	.3013105	-4.60	0.000	-1.97611	-.794995
gamma	.2501855	.0753835			.1386073	.4515835

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaxPeer worldbank trade infdi
age65 parties fhouse partdem deficit mcap gdpicap lngdp, nohr dist(gompertz)
```

Gompertz regression -- log relative-hazard form

```
No. of subjects =          58                Number of obs   =          803
No. of failures =          18
Time at risk    =          803
Log likelihood  = -14.058911                LR chi2(16)      =          39.38
                                                Prob > chi2     =          0.0010
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
peerprivat	-.0945198	.0970719	-0.97	0.330	-.2847771 .0957375	
LatinAm	-1.31783	1.878998	-0.70	0.483	-5.000598 2.364938	
EEurCentAs	-.5073125	1.982736	-0.26	0.798	-4.393404 3.378779	
LatAmxPeer	.1794368	.0955893	1.88	0.060	-.0079148 .3667884	
EECaxPeer	.1353885	.0968469	1.40	0.162	-.054428 .3252049	
(control variables omitted)						
gamma	.1749681	.1149338	1.52	0.128	-.0502981 .4002343	

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaxPeer worldbank trade infdi
age65 parties fhouse partdem deficit mcap gdpicap lngdp, dist(gamma)
```

Fitting constant-only model:

```
Iteration 0: log likelihood = -66.490766 (not concave)
Iteration 1: log likelihood = -40.072025
.
.
.
Iteration 12: log likelihood = -34.544303
```

Fitting full model:

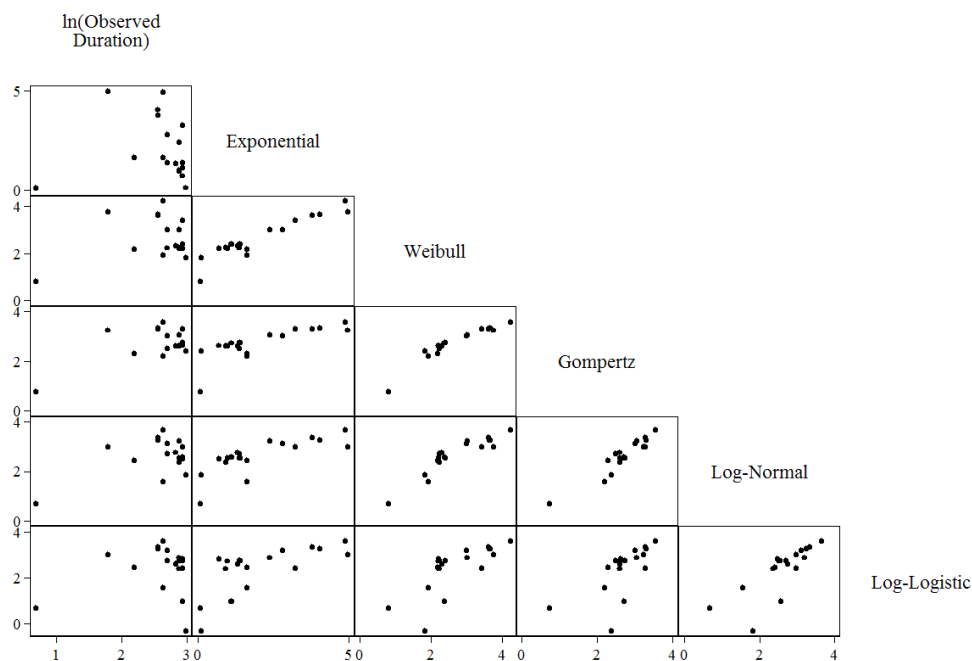
```
Iteration 0: log likelihood = -34.544303 (not concave)
Iteration 1: log likelihood = -30.529341 (not concave)
Iteration 2: log likelihood = -27.222987 (not concave)
Iteration 3: log likelihood = -25.569054 (not concave)
.
.
.
Iteration 24: log likelihood = -16.376731 (not concave)
Iteration 25: log likelihood = -16.254939 (not concave)
discontinuous region encountered
cannot compute an improvement
r(430);
```

## AIC & BIC

Table 1:  $\ln L$ , AIC, and BIC for Five Parametric Models

Model	$\ln L$	AIC	BIC
Exponential	-15.218	64.436	144.14
Weibull	-13.320	62.640	147.03
Gompertz	-14.059	64.118	148.51
Log-Normal	-15.224	66.447	150.84
Log-Logistic	-14.310	64.620	149.01

## Fitted Values



```
. corr ln_duration lnThat_E lnThat_W lnThat_G lnThat_LN lnThat_LL if fail==1
(obs=18)
```

	ln_dur~n	lnThat_E	lnThat_W	lnThat_G	lnThat~N	lnThat~L
ln_duration	1.0000					
lnThat_E	-0.0361	1.0000				
lnThat_W	0.2647	0.9398	1.0000			
lnThat_G	0.5873	0.7656	0.9294	1.0000		
lnThat_LN	0.4870	0.7522	0.9067	0.9423	1.0000	
lnThat_LL	0.1837	0.6758	0.7095	0.6644	0.7868	1.0000

## Hazard Ratios

```
. streg peerprivat LatinAm EEurCentAs LatAmxPeer EECaXPeer worldbank trade infdi
age65 parties fhouse partdem deficit mcap gdpicap lngdp, dist(weibull)
```

Weibull regression -- log relative-hazard form

```
No. of subjects =          58                Number of obs   =          803
No. of failures =          18
Time at risk    =          803
Log likelihood  = -13.319909                LR chi2(16)      =          43.42
                                                Prob > chi2     =          0.0002
```

_t	Haz. Ratio	Std. Err.	z	P> z	[95% Conf. Interval]	
peerprivat	.9501933	.0742503	-0.65	0.513	.8152618	1.107457
LatinAm	.4045029	.7392988	-0.50	0.620	.0112513	14.54251
EEurCentAs	1.416854	2.306705	0.21	0.831	.0582813	34.44461
LatAmxPeer	1.16952	.1031828	1.77	0.076	.9838049	1.390293
EECaXPeer	1.109824	.0960801	1.20	0.229	.9366203	1.315057
worldbank	.6006042	.2568022	-1.19	0.233	.259799	1.388479
trade	.9690452	.0153703	-1.98	0.047	.9393833	.9996437
infdi	1.217814	.1259195	1.91	0.057	.9944172	1.491398
age65	1.354827	.1825433	2.25	0.024	1.040391	1.764294
parties	1.762772	.553122	1.81	0.071	.9530294	3.260512
fhouse	3.716148	1.394028	3.50	0.000	1.781493	7.751787
partdem	.6515205	.0855734	-3.26	0.001	.5036488	.8428075
deficit	1.238215	.1344362	1.97	0.049	1.000873	1.531839
mcap	1.008013	.010827	0.74	0.457	.9870141	1.029458
gdpicap	.999944	.000127	-0.44	0.659	.9996952	1.000193
lngdp	1.296133	.3975817	0.85	0.398	.7104736	2.364563
/ln_p	.6882986	.293876	2.34	0.019	.1123122	1.264285
p	1.990326	.5849091			1.118862	3.54056
1/p	.5024302	.1476522			.2824412	.8937652

### Linear Combinations of Parameters:

```
. lincom(peerprivat+LatAmxPeer)
```

```
( 1)  [_t]peerprivat + [_t]LatAmxPeer = 0
```

	_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
(1)		.1055036	.0457227	2.31	0.021	.0158887	.1951185

```
. lincom(peerprivat+EECAxPeer)
```

```
( 1)  [_t]peerprivat + [_t]EECAxPeer = 0
```

	_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
(1)		.0531117	.0448715	1.18	0.237	-.0348348	.1410581

### Nonlinear Combinations of Parameters:

```
. nlcom(exp(_b[peerprivat]+_b[LatAmxPeer]))
```

```
_nl_1:  exp(_b[peerprivat]+_b[LatAmxPeer])
```

	_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
_nl_1		1.11127	.0508103	21.87	0.000	1.011684	1.210856

```
. nlcom(exp(_b[peerprivat]+_b[EECAxPeer]))
```

```
_nl_1:  exp(_b[peerprivat]+_b[EECAxPeer])
```

	_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
_nl_1		1.054547	.0473191	22.29	0.000	.9618037	1.147291



Predicted Hazard and Survival Curves

Figure 6: Predicted Survival Curve, at  $\bar{X}\hat{\beta}$

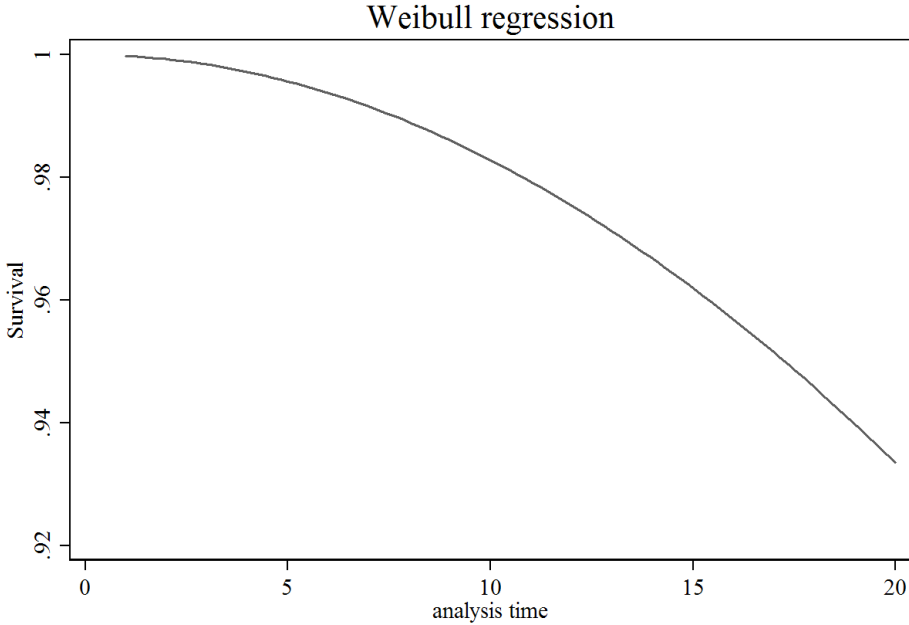


Figure 7: Predicted Hazards for Three Peer Groups, at Group-Specific Means

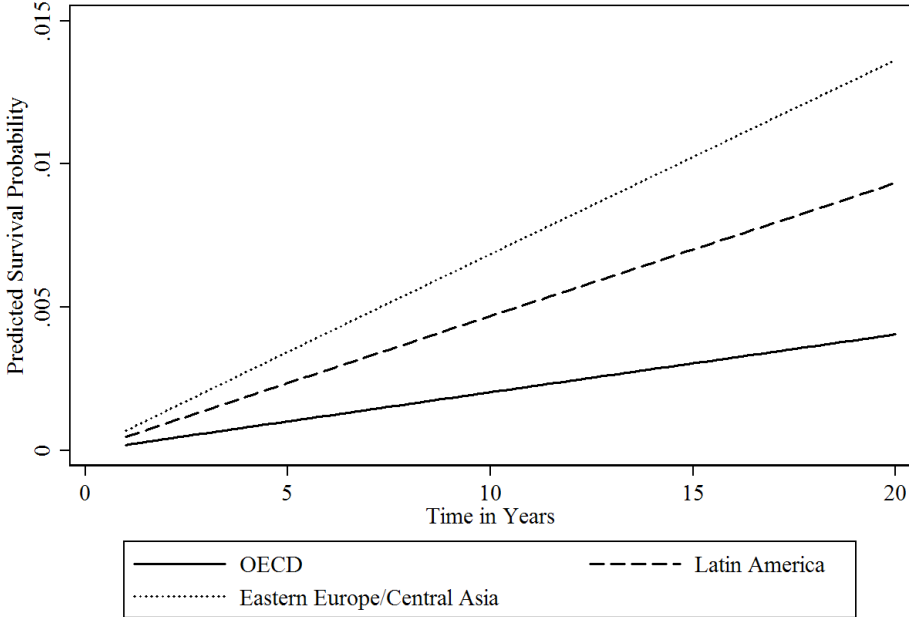


Figure 8: Predicted Survival Curves for Three Peer Groups, at Group-Specific Means

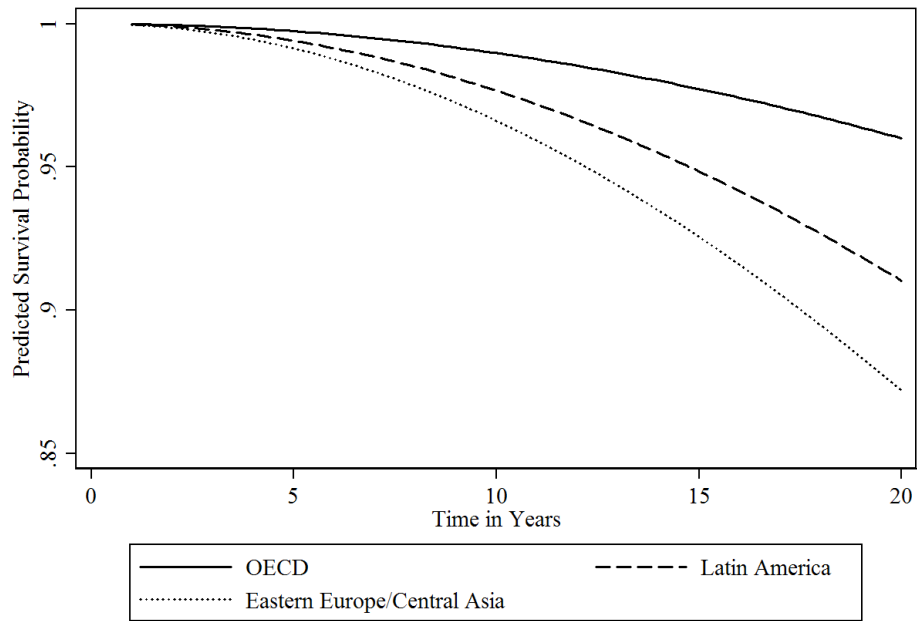
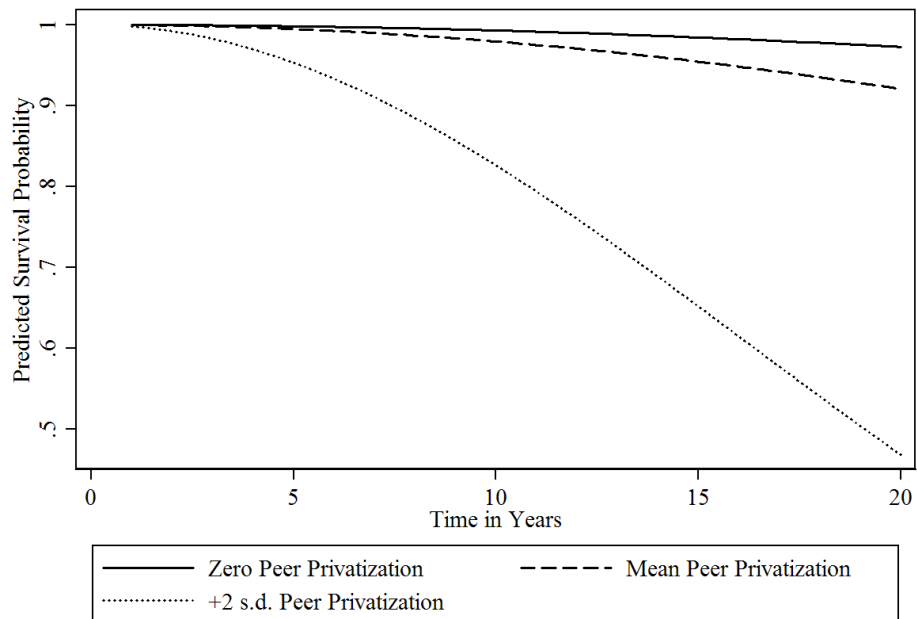


Figure 9: Predicted Survival Curves for Latin American Countries, at Three Levels of *Peer Privatization*



Data: Dyadic Interstate Disputes, 1950-1985

. su duration dispute allies contig capratio growth democ trade

Variable	Obs	Mean	Std. Dev.	Min	Max
duration	20448	14.18574	8.804608	1	35
dispute	20448	.0198063	.1393377	0	1
allies	20448	.3563185	.4789226	0	1
contig	20448	.3098592	.4624467	0	1
capratio	20448	1.667739	4.478851	.01	78.9296
growth	20448	.0078229	.0335592	-.2649	.1647
democ	20448	-.3437549	.6954232	-1	1
trade	20448	.0023101	.008264	0	.1768

. stdes

failure \_d: dispute  
analysis time \_t: duration  
enter on or after: time start

Category	total	per subject			
		mean	min	median	max
no. of subjects	20448				
no. of records	20448	1	1	1	1
(first) entry time		13.18574	0	12	34
(final) exit time		14.18574	1	13	35
subjects with gap	0				
time on gap if gap	0				
time at risk	20448	1	1	1	1
failures	405	.0198063	0	0	1

**Basic Cox Model (Efron Method for Ties):**

```
. stcox allies contig capratio growth democ trade, nohr efron bases(basicS)
basehc(basich)
```

Cox regression -- Efron method for ties

```
No. of subjects =          20448          Number of obs   =          20448
No. of failures =           405
Time at risk    =          20448
Log likelihood  = -2501.8834          LR chi2(6)       =          272.35
                                          Prob > chi2      =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4141413	.1107106	-3.74	0.000	-.6311301	-.1971526
contig	1.213475	.120933	10.03	0.000	.9764511	1.4505
capratio	-.2142166	.0514351	-4.16	0.000	-.3150276	-.1134056
growth	-3.227159	1.22786	-2.63	0.009	-5.633721	-.8205979
democ	-.4394706	.0997931	-4.40	0.000	-.6350616	-.2438797
trade	-13.16247	10.32656	-1.27	0.202	-33.40216	7.077214

**Hazard Ratios**

```
. stcox
```

Cox regression -- Efron method for ties

```
No. of subjects =          20448          Number of obs   =          20448
No. of failures =           405
Time at risk    =          20448
Log likelihood  = -2501.8834          LR chi2(6)       =          272.35
                                          Prob > chi2      =          0.0000
```

_t	Haz. Ratio	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	.6609075	.0731695	-3.74	0.000	.5319903	.8210654
contig	3.36516	.4069588	10.03	0.000	2.655017	4.265245
capratio	.8071736	.0415171	-4.16	0.000	.7297688	.8927885
growth	.03967	.0487092	-2.63	0.009	.0035752	.4401684
democ	.6443774	.0643044	-4.40	0.000	.5299029	.7835819
trade	1.92e-06	.0000198	-1.27	0.202	3.12e-15	1184.663

## An Illustration of the Effect of “Ties”

```
. stcox allies contig capratio growth democ trade, nohr
```

```
Cox regression -- Breslow method for ties
```

```
No. of subjects =          20448                Number of obs   =          20448
No. of failures =           405
Time at risk    =          20448
Log likelihood  = -2510.7156                    LR chi2(6)       =          264.75
                                                Prob > chi2      =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
allies	-.4005594	.110695	-3.62	0.000	-.6175176 -.1836013
contig	1.193988	.1208723	9.88	0.000	.9570829 1.430894
capratio	-.2109814	.0511536	-4.12	0.000	-.3112405 -.1107223
growth	-3.126839	1.227503	-2.55	0.011	-5.532701 -.7209763
democ	-.434744	.0999085	-4.35	0.000	-.6305612 -.2389269
trade	-13.06191	10.28504	-1.27	0.204	-33.22023 7.096406

```
. stset untied_duration, fail(dispute) en(untied_start)
<output omitted>
```

```
. stcox allies contig capratio growth democ trade, nohr
```

```
Cox regression -- no ties
```

```
No. of subjects =          20448                Number of obs   =          20448
No. of failures =           405
Time at risk    = 20449.21692
Log likelihood  = -2501.1676                    LR chi2(6)       =          269.77
                                                Prob > chi2      =          0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
allies	-.4219632	.1107677	-3.81	0.000	-.6390639 -.2048625
contig	1.222924	.1209401	10.11	0.000	.9858857 1.459962
capratio	-.2068422	.0509056	-4.06	0.000	-.3066153 -.1070691
growth	-3.500547	1.234624	-2.84	0.005	-5.920365 -1.080729
democ	-.430965	.1003055	-4.30	0.000	-.6275602 -.2343697
trade	-14.49323	10.52374	-1.38	0.168	-35.11939 6.132917

“Exact” Methods for Ties

. stcox allies contig capratio growth democ trade, nohr exactp

Cox regression -- exact partial likelihood

```
No. of subjects =      20448                Number of obs   =      20448
No. of failures =         405
Time at risk    =      20448
Log likelihood  =  -1726.7658                LR chi2(6)      =      272.57
                                                Prob > chi2     =      0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4204018	.11343	-3.71	0.000	-.6427206	-.198083
contig	1.237777	.1228533	10.08	0.000	.9969887	1.478565
capratio	-.2151302	.0516297	-4.17	0.000	-.3163226	-.1139379
growth	-3.3322	1.267388	-2.63	0.009	-5.816235	-.8481654
democ	-.4475007	.1012385	-4.42	0.000	-.6459244	-.249077
trade	-13.55219	10.43382	-1.30	0.194	-34.00211	6.897731

. stcox allies contig capratio growth democ trade, nohr exactm

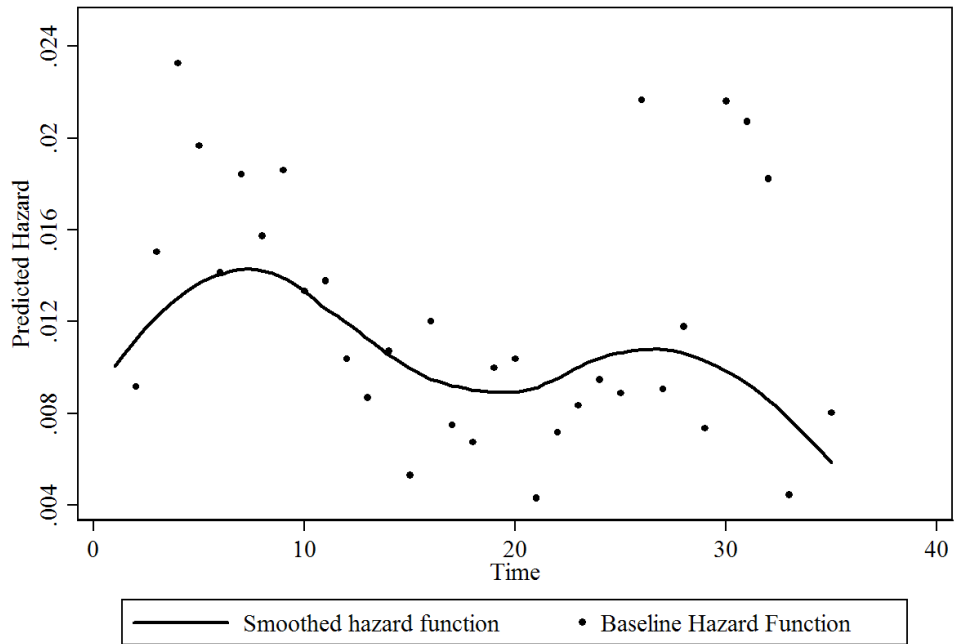
Cox regression -- exact marginal likelihood

```
No. of subjects =      20448                Number of obs   =      20448
No. of failures =         405
Time at risk    =      20448
Log likelihood  =  -1726.9865                LR chi2(6)      =      272.54
                                                Prob > chi2     =      0.0000
```

_t	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4146707	.1107262	-3.75	0.000	-.6316901	-.1976514
contig	1.213951	.1209406	10.04	0.000	.9769113	1.45099
capratio	-.2143322	.0514458	-4.17	0.000	-.315164	-.1135003
growth	-3.232832	1.228313	-2.63	0.008	-5.640281	-.8253836
democ	-.4396288	.0997959	-4.41	0.000	-.6352251	-.2440325
trade	-13.15716	10.32803	-1.27	0.203	-33.39971	7.085402

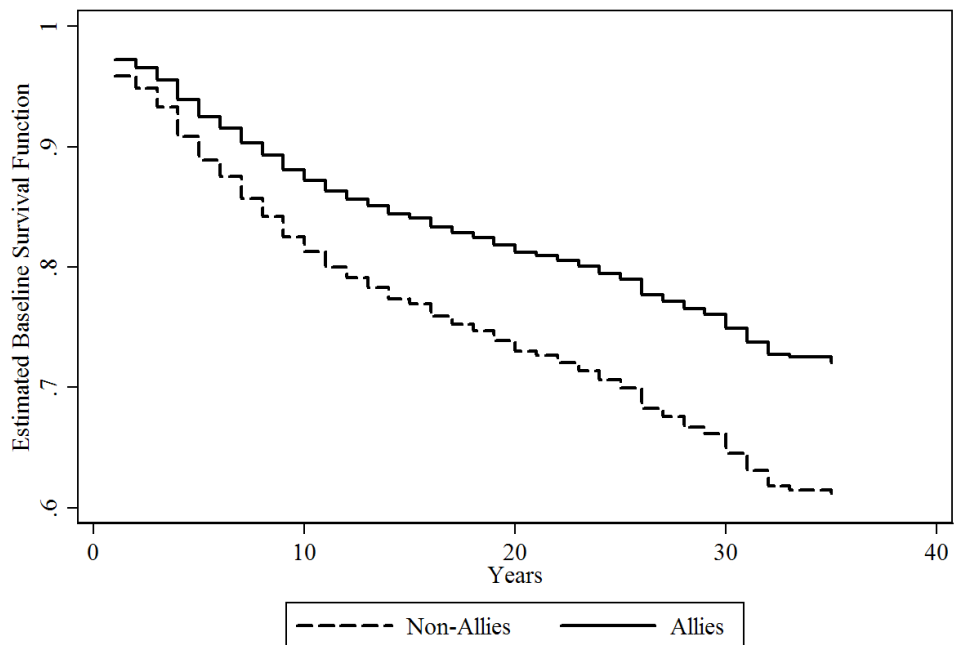
## Plotting the Baseline Hazard

Figure 10: Predicted Survival Curves for *Allies*=0 and *Allies*=1



## Comparing Predicted Survival Curves

Figure 11: Predicted Survival Curves for *Allies*=0 and *Allies*=1



## Robust/Sandwich Variance Estimates

```
. stcox allies contig capratio growth democ trade, nohr efron robust
```

```
Cox regression -- Efron method for ties
```

```
No. of subjects      =          20448          Number of obs      =          20448
No. of failures      =             405
Time at risk         =          20448
Log pseudolikelihood = -2501.8834
Wald chi2(6)         =          203.10
Prob > chi2          =           0.0000
```

_t	Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4141413	.1133494	-3.65	0.000	-.6363021	-.1919805
contig	1.213475	.1266108	9.58	0.000	.9653229	1.461628
capratio	-.2142166	.0632447	-3.39	0.001	-.3381738	-.0902593
growth	-3.227159	1.301138	-2.48	0.013	-5.777344	-.6769749
democ	-.4394706	.0951549	-4.62	0.000	-.6259708	-.2529705
trade	-13.16247	11.40692	-1.15	0.249	-35.51963	9.194679

```
. stcox allies contig capratio growth democ trade, nohr efron robust cluster(dyadid)
```

```
Cox regression -- Efron method for ties
```

```
No. of subjects      =          20448          Number of obs      =          20448
No. of failures      =             405
Time at risk         =          20448
Log pseudolikelihood = -2501.8834
Wald chi2(6)         =           92.92
Prob > chi2          =           0.0000
(Std. Err. adjusted for 827 clusters in dyadid)
```

_t	Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4141413	.1704406	-2.43	0.015	-.7481988	-.0800839
contig	1.213475	.1782591	6.81	0.000	.864094	1.562857
capratio	-.2142166	.081796	-2.62	0.009	-.3745337	-.0538994
growth	-3.227159	1.317689	-2.45	0.014	-5.809782	-.6445371
democ	-.4394706	.1231521	-3.57	0.000	-.6808444	-.1980969
trade	-13.16247	13.82712	-0.95	0.341	-40.26313	13.93818



## Some R Examples

*Model Estimation:*

```
> robustCox<-coxph(Surv(start, duration, dispute)~allies +
contig + capratio + growth + democ + trade, data=Day50R,
na.action=na.exclude, method="efron", robust=TRUE)
```

```
> summary(robustCox)
```

Call:

```
coxph(formula = Surv(start, duration, dispute) ~ allies + contig +
  capratio + growth + democ + trade, data = Day50R, na.action = na.exclude,
  method = "efron", robust = TRUE)
```

n= 20448

	coef	exp(coef)	se(coef)	robust se	z	p
allies	-0.414	6.61e-01	0.1107	0.1133	-3.65	2.6e-04
contig	1.213	3.37e+00	0.1209	0.1266	9.58	0.0e+00
capratio	-0.214	8.07e-01	0.0514	0.0632	-3.39	7.1e-04
growth	-3.227	3.97e-02	1.2279	1.3011	-2.48	1.3e-02
democ	-0.439	6.44e-01	0.0998	0.0952	-4.62	3.9e-06
trade	-13.162	1.92e-06	10.3266	11.4066	-1.15	2.5e-01

	exp(coef)	exp(-coef)	lower .95	upper .95
allies	6.61e-01	1.51e+00	5.29e-01	0.825
contig	3.37e+00	2.97e-01	2.63e+00	4.313
capratio	8.07e-01	1.24e+00	7.13e-01	0.914
growth	3.97e-02	2.52e+01	3.10e-03	0.508
democ	6.44e-01	1.55e+00	5.35e-01	0.776
trade	1.92e-06	5.20e+05	3.75e-16	9839.225

Rsquare= 0.013 (max possible= 0.227 )

Likelihood ratio test= 272 on 6 df, p=0

Wald test = 203 on 6 df, p=0

Score (logrank) test = 262 on 6 df, p=0, Robust = 221 p=0

(Note: the likelihood ratio and score tests assume independence of observations within a cluster, the Wald and robust score tests do not).

*Robust/Sandwich Variance Estimates:*

```
> clusterCox<-coxph(Surv(start, duration, dispute)~allies + contig + capratio + growth +  
democ + trade + cluster(dyadid), data=Day50R, na.action=na.exclude, method="efron")
```

```
> summary(clusterCox)
```

Call:

```
coxph(formula = Surv(start, duration, dispute) ~ allies + contig +  
      capratio + growth + democ + trade + cluster(dyadid), data = Day50R,  
      na.action = na.exclude, method = "efron")
```

n= 20448

	coef	exp(coef)	se(coef)	robust se	z	p
allies	-0.414	6.61e-01	0.1107	0.1703	-2.431	1.5e-02
contig	1.213	3.37e+00	0.1209	0.1782	6.811	9.7e-12
capratio	-0.214	8.07e-01	0.0514	0.0817	-2.620	8.8e-03
growth	-3.227	3.97e-02	1.2279	1.3169	-2.451	1.4e-02
democ	-0.439	6.44e-01	0.0998	0.1231	-3.571	3.6e-04
trade	-13.162	1.92e-06	10.3266	13.8188	-0.953	3.4e-01

	exp(coef)	exp(-coef)	lower .95	upper .95
allies	6.61e-01	1.51e+00	4.73e-01	9.23e-01
contig	3.37e+00	2.97e-01	2.37e+00	4.77e+00
capratio	8.07e-01	1.24e+00	6.88e-01	9.47e-01
growth	3.97e-02	2.52e+01	3.00e-03	5.24e-01
democ	6.44e-01	1.55e+00	5.06e-01	8.20e-01
trade	1.92e-06	5.20e+05	3.32e-18	1.11e+06

Rsquare= 0.013 (max possible= 0.227 )

Likelihood ratio test= 272 on 6 df, p=0

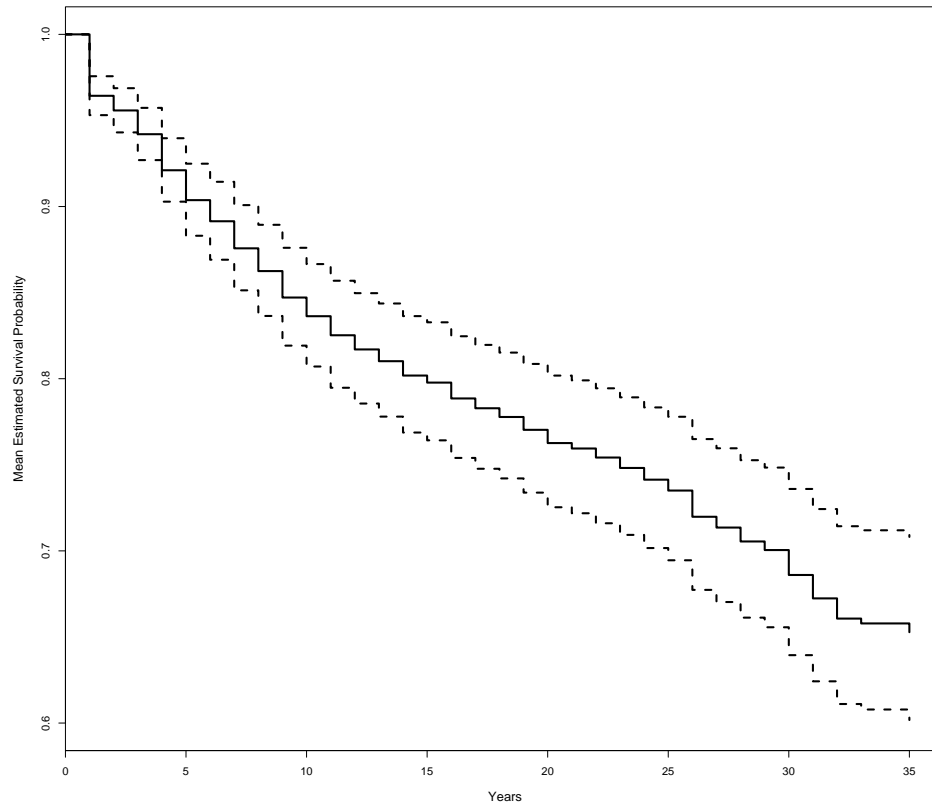
Wald test = 93 on 6 df, p=0

Score (logrank) test = 262 on 6 df, p=0, Robust = 78.2 p=8.33e-15

(Note: the likelihood ratio and score tests assume independence of observations within a cluster, the Wald and robust score tests do not).

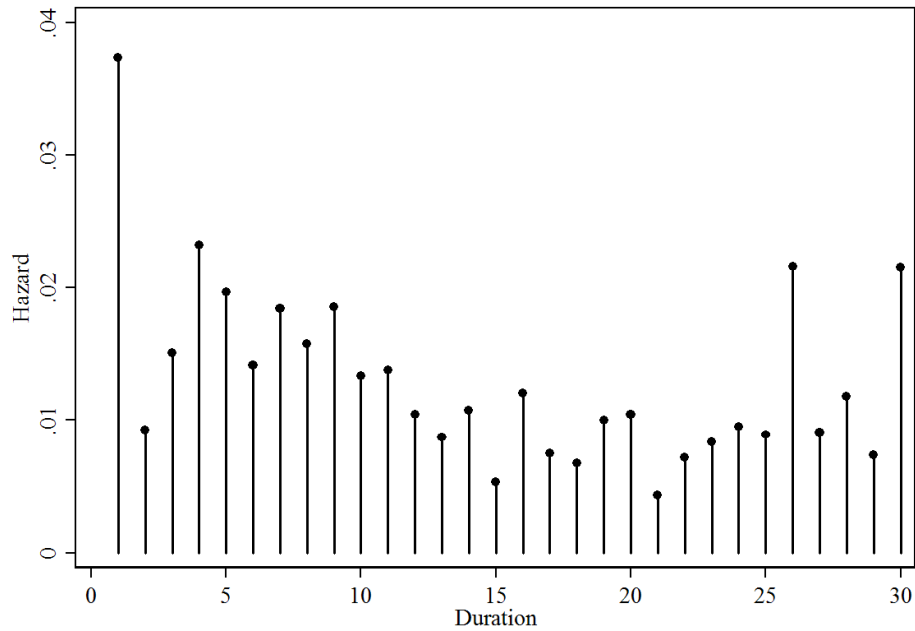
*Plotting Predicted Mean Survival:*

```
> plot(survfit(robustCox), ylim=c(.6,1), xlab='Years', ylab='Mean Estimated  
Survival Probability', lwd=3, cex.lab=1.2)
```



## Discrete-Time Approaches

Figure 12: A Discrete Hazard Function



## A Few Logit Analyses

```
. logit dispute allies contig capratio growth democ trade
```

```
Logistic regression                Number of obs   =       20448
                                   LR chi2(6)         =       284.79
                                   Prob > chi2         =       0.0000
Log likelihood = -1846.8783         Pseudo R2      =       0.0716
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
allies	-.4796863	.1127463	-4.25	0.000	-.7006649 -.2587076
contig	1.353576	.1209052	11.20	0.000	1.116606 1.590546
capratio	-.1961988	.0501055	-3.92	0.000	-.2944037 -.0979938
growth	-3.42753	1.251813	-2.74	0.006	-5.881038 -.9740222
democ	-.4011976	.1006345	-3.99	0.000	-.5984376 -.2039576
trade	-21.07611	11.30396	-1.86	0.062	-43.23146 1.079242
_cons	-4.326677	.1145089	-37.78	0.000	-4.55111 -4.102243

```
. logit dispute allies contig capratio growth democ trade duration
```

```
Logistic regression                Number of obs =    20448
                                   LR chi2(7)      =    315.04
                                   Prob > chi2     =    0.0000
Log likelihood = -1831.7544        Pseudo R2      =    0.0792
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
allies	-.4372892	.1133989	-3.86	0.000	-.6595469 - .2150315
contig	1.237468	.1231841	10.05	0.000	.9960314 1.478904
capratio	-.2221353	.0522061	-4.25	0.000	-.3244573 -.1198133
growth	-3.906579	1.24168	-3.15	0.002	-6.340227 -1.47293
democ	-.3897999	.0993313	-3.92	0.000	-.5844857 -.1951141
trade	-12.52205	10.5063	-1.19	0.233	-33.11402 8.069913
duration	-.0348606	.0064981	-5.36	0.000	-.0475967 -.0221245
_cons	-3.831356	.1422191	-26.94	0.000	-4.110101 -3.552612

```
. logit dispute allies contig capratio growth democ trade duration durationsq
duration3 duration4
```

```
Logistic regression                Number of obs =    20448
                                   LR chi2(10)     =    335.03
                                   Prob > chi2     =    0.0000
Log likelihood = -1821.7585        Pseudo R2      =    0.0842
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]
allies	-.4264649	.1133056	-3.76	0.000	-.6485398 -.2043899
contig	1.236488	.1228581	10.06	0.000	.9956904 1.477285
capratio	-.2164406	.0516908	-4.19	0.000	-.3177528 -.1151285
growth	-3.662032	1.258202	-2.91	0.004	-6.128062 -1.196002
democ	-.4367741	.1010708	-4.32	0.000	-.6348692 -.238679
trade	-13.32134	10.45781	-1.27	0.203	-33.81826 7.175589
duration	.0125515	.0967292	0.13	0.897	-.1770342 .2021372
durationsq	-.0154883	.0122938	-1.26	0.208	-.0395837 .008607
duration3	.0008897	.0005698	1.56	0.118	-.0002271 .0020065
duration4	-.0000137	8.63e-06	-1.59	0.112	-.0000306 3.21e-06
_cons	-3.712094	.24111	-15.40	0.000	-4.184661 -3.239527

```
. testparm durat*
```

- ( 1) duration = 0
- ( 2) durationsq = 0
- ( 3) duration3 = 0
- ( 4) duration4 = 0

```
chi2( 4) = 51.06
Prob > chi2 = 0.0000
```

```
. xi i.duration
i.duration      _Iduration_1-35      (naturally coded; _Iduration_1 omitted)

. logit dispute allies contig capratio growth democ trade _Iduration_2 - _Iduration_33
_Iduration_35
```

```
Logistic regression                                Number of obs =      20448
                                                    LR chi2(39)      =      375.92
                                                    Prob > chi2      =      0.0000
Log likelihood = -1801.3137                        Pseudo R2       =      0.0945
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4314486	.1134293	-3.80	0.000	-.6537659	-.2091313
contig	1.26358	.1225534	10.31	0.000	1.02338	1.503781
capratio	-.2093872	.0510959	-4.10	0.000	-.3095332	-.1092411
growth	-3.404787	1.275106	-2.67	0.008	-5.903948	-.9056258
democ	-.4634443	.1017302	-4.56	0.000	-.6628319	-.2640567
trade	-14.78303	10.54518	-1.40	0.161	-35.45121	5.885155
_Iduration_2	-1.319414	.3285792	-4.02	0.000	-1.963417	-.6754108
<output omitted>						
_Iduratio~33	-2.029241	1.016382	-2.00	0.046	-4.021313	-.0371691
_Iduratio~35	-1.418437	1.020086	-1.39	0.164	-3.417769	.5808961
_cons	-3.401713	.180382	-18.86	0.000	-3.755255	-3.048171

```
. testparm _I*

( 1) _Iduration_2 = 0
( 2) _Iduration_3 = 0
.
.
.
<output omitted>
.
.
.
(32) _Iduration_33 = 0
(33) _Iduration_35 = 0
```

```
chi2( 33) = 89.06
Prob > chi2 = 0.0000
```

Figure 13: Predicted Mean Hazards, Discrete-Time (Logit) Models

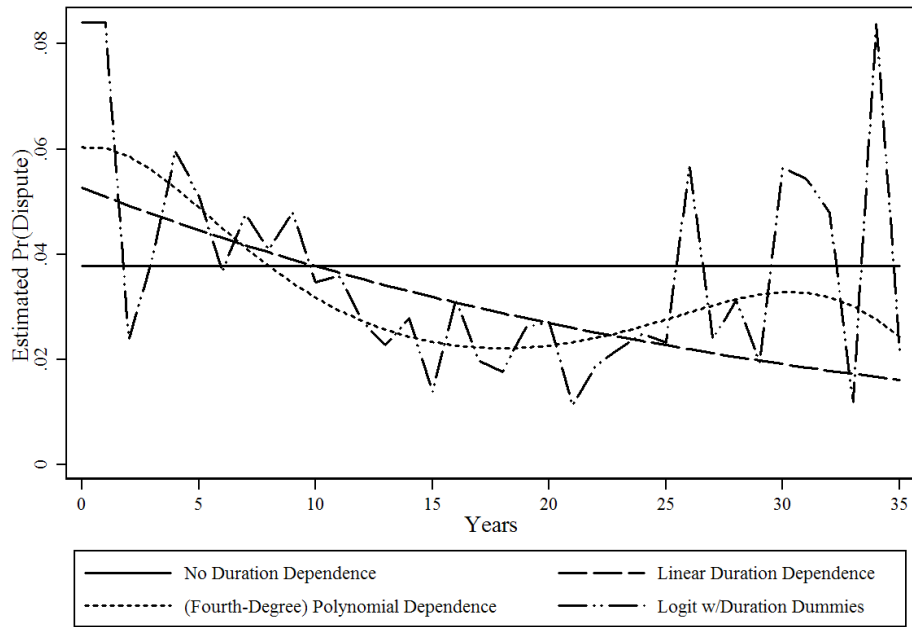
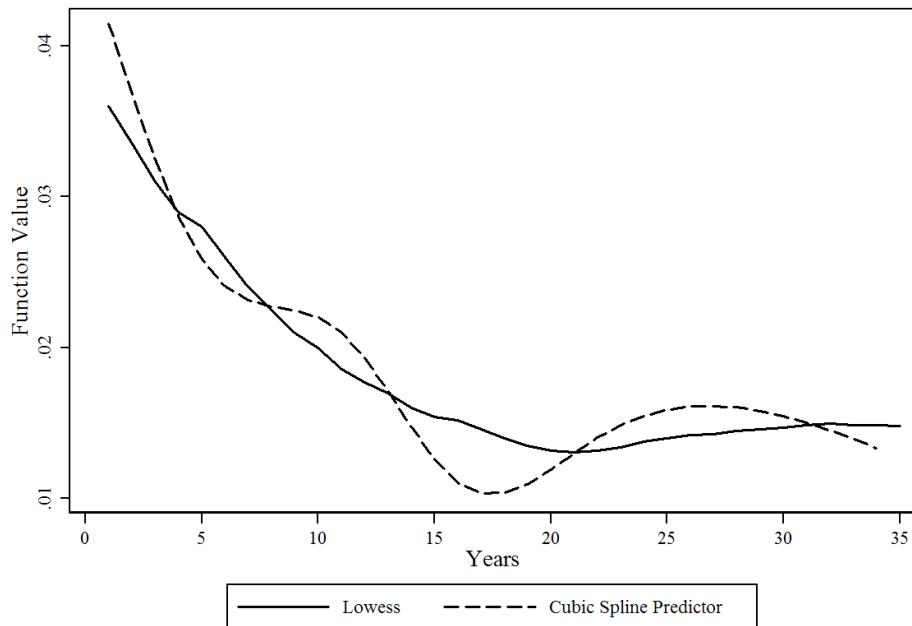


Figure 14: Lowess and Cubic Spline Functions of dispute on duration



```
. lowess dispute duration, adjust nograph gen(lowessDur)
```

```
. logit dispute allies contig capratio growth democ trade lowessDur
```

```
Logistic regression                               Number of obs =      20448
                                                    LR chi2(7)      =      333.04
                                                    Prob > chi2     =      0.0000
Log likelihood = -1822.7544                       Pseudo R2      =      0.0837
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4213745	.1133634	-3.72	0.000	-.6435626	-.1991864
contig	1.222782	.1226094	9.97	0.000	.9824719	1.463092
capratio	-.221008	.0519247	-4.26	0.000	-.3227787	-.1192374
growth	-3.618861	1.241322	-2.92	0.004	-6.051808	-1.185915
democ	-.4240152	.0998594	-4.25	0.000	-.619736	-.2282944
trade	-12.2739	10.33369	-1.19	0.235	-32.52757	7.979765
lowessDur	46.89038	6.577867	7.13	0.000	33.998	59.78277
_cons	-5.282134	.1825519	-28.93	0.000	-5.639929	-4.924339

```
. spline dispute duration, n(4) gen(newspline) nograph
```

```
. logit dispute allies contig capratio growth democ trade newspline
```

```
Logistic regression                               Number of obs =      20448
                                                    LR chi2(7)      =      334.15
                                                    Prob > chi2     =      0.0000
Log likelihood = -1822.1979                       Pseudo R2      =      0.0840
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4205267	.1133223	-3.71	0.000	-.6426344	-.198419
contig	1.230388	.1223423	10.06	0.000	.9906017	1.470175
capratio	-.2181174	.0516733	-4.22	0.000	-.3193953	-.1168395
growth	-3.423613	1.239825	-2.76	0.006	-5.853625	-.9936014
democ	-.4302531	.1000463	-4.30	0.000	-.6263402	-.2341661
trade	-12.9469	10.39186	-1.25	0.213	-33.31458	7.420777
newspline	39.65726	5.464181	7.26	0.000	28.94766	50.36686
_cons	-5.147013	.1666201	-30.89	0.000	-5.473583	-4.820444



```
. rc_spline duration, nk(4)
number of knots = 4
value of knot 1 = 2
value of knot 2 = 9
value of knot 3 = 18
value of knot 4 = 30
```

```
. logit dispute allies contig capratio growth democ trade _Sduration1 _Sduration2
_Sduration3
```

```
Logistic regression                                Number of obs =      20448
                                                    LR chi2(9)      =      334.50
                                                    Prob > chi2     =      0.0000
Log likelihood = -1822.0226                       Pseudo R2       =      0.0841
```

dispute	Coef.	Std. Err.	z	P> z	[95% Conf. Interval]	
allies	-.4271112	.1133278	-3.77	0.000	-.6492297	-.2049927
contig	1.235308	.1228487	10.06	0.000	.9945287	1.476087
capratio	-.2168885	.0516832	-4.20	0.000	-.3181858	-.1155913
growth	-3.68127	1.256232	-2.93	0.003	-6.14344	-1.2191
democ	-.442577	.1011338	-4.38	0.000	-.6407955	-.2443584
trade	-12.98309	10.39775	-1.25	0.212	-33.3623	7.396126
_Sduration1	-.0675975	.027676	-2.44	0.015	-.1218415	-.0133535
_Sduration2	-.0280649	.1328698	-0.21	0.833	-.2884848	.2323551
_Sduration3	.2396889	.3030326	0.79	0.429	-.3542441	.8336218
_cons	-3.628666	.1792857	-20.24	0.000	-3.98006	-3.277273

```
. testparm _S*
```

- ( 1) \_Sduration1 = 0
- ( 2) \_Sduration2 = 0
- ( 3) \_Sduration3 = 0

```
chi2( 3) = 49.91
Prob > chi2 = 0.0000
```

Figure 15: Mean Predicted Hazards, Lowess and Cubic Spline Models

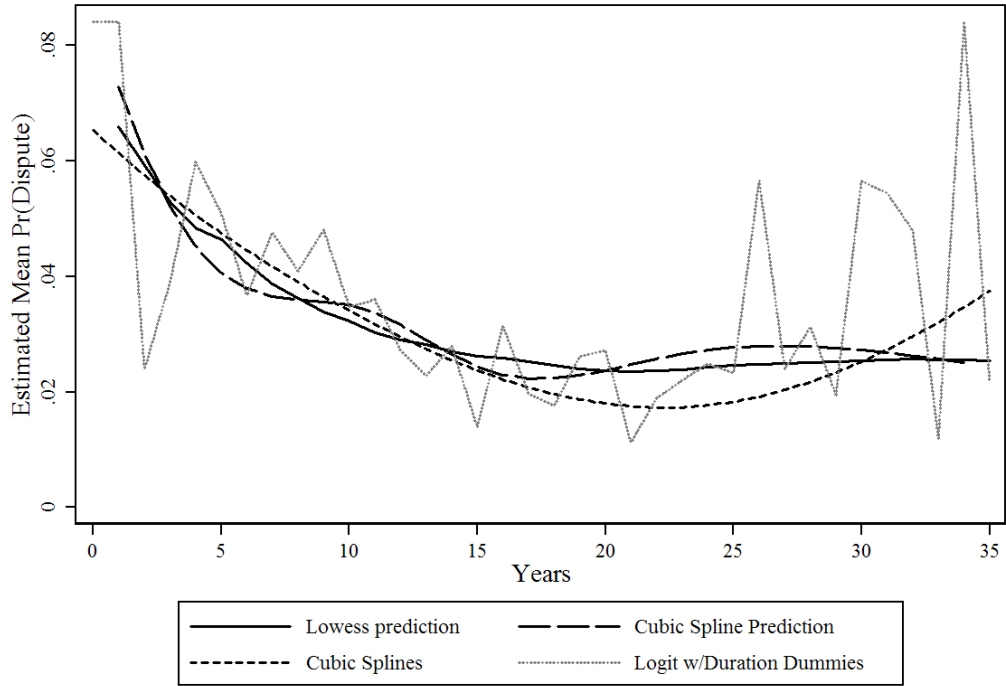


Table 2: AIC and BIC Values, Discrete-Time (Logit) Models

Model	$\ln L$	d.f.	AIC	BIC
No Dependence / "Flat"	-1846.88	7	3707.8	3763.2
Linear	-1831.75	8	3679.5	3742.9
Polynomial	-1821.76	11	3665.5	3752.7
"Duration Dummies"	-1801.31	40	3682.6	3999.7
Lowess	-1822.75	8	3661.5	3724.9
Cubic Spline (linear predictor)	-1822.20	8	3660.4	3723.8
Cubic Splines	-1822.02	10	3664.0	3743.3

## Cox/Poisson Equivalence

```
. stcox allies contig capratio growth democ trade, nohr
```

```
Cox regression -- Breslow method for ties
```

```
No. of subjects =      20448                Number of obs   =      20448
No. of failures =         405
Time at risk    =      20448
Log likelihood   =  -2510.7156                LR chi2(6)      =      264.75
                                                Prob > chi2     =      0.0000
```

```
-----+-----
      _t |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-----+-----
      allies |  -.4005594   .110695   -3.62   0.000   - .6175176   - .1836013
      contig |   1.193988   .1208723   9.88   0.000    .9570829    1.430894
  capratio |  -.2109814   .0511536   -4.12   0.000   - .3112405   - .1107223
      growth |  -3.126839   1.227503   -2.55   0.011   -5.532701   - .7209763
      democ |  -.434744    .0999085   -4.35   0.000   - .6305612   - .2389269
      trade | -13.06191   10.28504   -1.27   0.204   -33.22023    7.096406
-----+-----
```

```
. xi: poisson dispute allies contig capratio growth democ trade i.duration
```

```
i.duration      _Iduration_1-35      (naturally coded; _Iduration_1 omitted)
```

```
Poisson regression                Number of obs   =      20448
                                   LR chi2(40)        =      377.70
                                   Prob > chi2         =      0.0000
Log likelihood = -1804.4594        Pseudo R2       =      0.0947
```

```
-----+-----
      dispute |      Coef.   Std. Err.      z    P>|z|     [95% Conf. Interval]
-----+-----
      allies |  -.4005639   .1106933   -3.62   0.000   - .6175188   - .183609
      contig |   1.193975   .1208705   9.88   0.000    .9570728    1.430877
  capratio |  -.2109975   .0511552   -4.12   0.000   - .3112598   - .1107352
      growth |  -3.126931   1.227476   -2.55   0.011   -5.53274    - .7211224
      democ |  -.4347376   .0999067   -4.35   0.000   - .6305512   - .238924
      trade | -13.06209   10.28493   -1.27   0.204   -33.22018    7.095995
  _Iduration_2 | -1.368926   .3219423   -4.25   0.000   -1.999921   - .7379303
  _Iduration_3 |  -.8832507   .2705674   -3.26   0.001   -1.413553   - .3529484
<output omitted>
  _Iduratio~34 | -14.68867   608.7769   -0.02   0.981   -1207.87    1178.492
  _Iduratio~35 |  -1.496368   1.012187   -1.48   0.139   -3.480219    .4874817
      _cons |  -3.325521   .1775939  -18.73   0.000   -3.673598   -2.977443
-----+-----
```